Jakarta International School

8th Grade – AG1

Practice Test - Black

Points, Lines, and Planes

Name: _____

Date: _____

Score: ___/40

Goal 5: Solve problems using visualization and geometric modeling

Section 1: ***Points, Lines, and Planes***

Read the following statements and indicate if each of the following is ALWAYS TRUE **(A)**, SOMETIMES TRUE **(S)** or NEVER TRUE **(N).** (4 points)

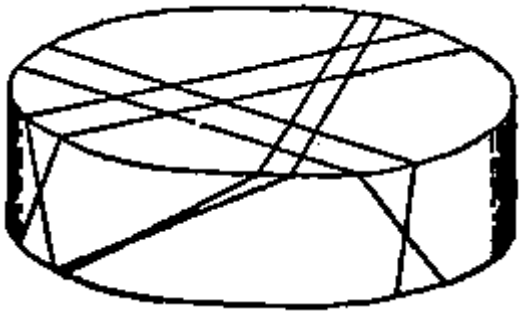
Justify your answer either by a written explanation **or** a drawing to show your understanding.

#	Statement	A/S/N	Drawing or Explanation
1.	$\overleftrightarrow{AC}$ and $\overleftrightarrow{CD}$ are different lines		
2.	If l is a line parallel to the plane *A* and B is a plane containing the line l, then planes *A* and B are parallel		

3. How many regions would be formed by n lines? Clearly explain or show how you arrive at your answer. (2 points)

4. Who cut the cheese? The soldier Cut the Cheese! (3 points)

   A soldier cut a brick of cheese to share with his platoon. How many pieces of cheese did the soldier produce with six plane cuts?



The cheese is divided in two pieces by one cut, 4 by the second, 8 by the third, 15 by the fourth, 26 by the fifth, and 42 by the sixth.

QUESTIONS 5 - 8 concern your understanding of SPHERICAL GEOMETRY

5. For each property listed from plane Euclidean Geometry, write a corresponding statement for spherical geometry. (2 points each = 6 points)

   a. The shortest path between two points is a straight line segment.

   b. Two lines intersecting to form four right angles are perpendicular.

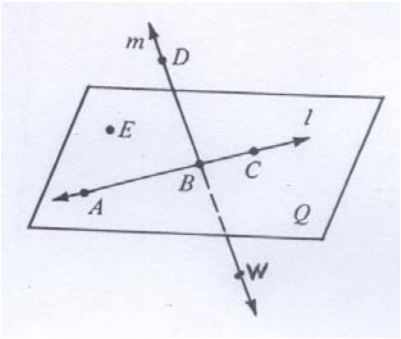
   c. Through any two points in a plane, there is a unique and infinite straight line.

6. Compare the distance between any pole point and its equator to the length of a great circle on the same sphere. (2 points)

7. Compare and contrast lines in plane Euclidean Geometry with great circles in spherical geometry. Consider the number and type of regions created when the "line" divides the "plane." Also, consider the number of intersection points with other "lines." (2 points)

8. Is it possible for parallel great circles to exist? Explain. (2 points)

Distance, Line Segments, and Rays



9. Do the two figures named intersect? If so, what is the intersection? (2 points)

$\overrightarrow{AB}$ and $\overrightarrow{CB}$?

$\overrightarrow{DB}$ and $\overleftrightarrow{BW}$?

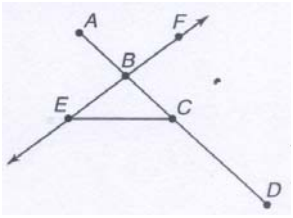
10. Point C lies on $\overline{AB}$ such that $AC = \frac{1}{4}AB$. If the endpoints of $\overline{AB}$ are $A(8,12)$ and $B(-4,0)$, find the coordinates of C. (2 points)

11. 2 points, A and B, are on a number line. Write an expression that represents the *distance* between the two points. (1 point)

12. Find the value(s) of x satisfying the equation $|x-1|=2|x-3|$. Draw a number line that illustrates why your answer makes sense. (3 points)

Midpoints

13. In the figure below, $\overline{EC}$ bisects $\overline{AD}$ at C, and $\overline{EF}$ bisects $\overline{AC}$ at B. Find the value of x and the measure of the indicated segment. (2 points)



$AD=12x-10, AC=3-2x; \overline{BC}$

14. If $R(2,5)$ is the midpoint of ST and the coordinates of T are $(-1,8)$, find the coordinates of S. (2 points)

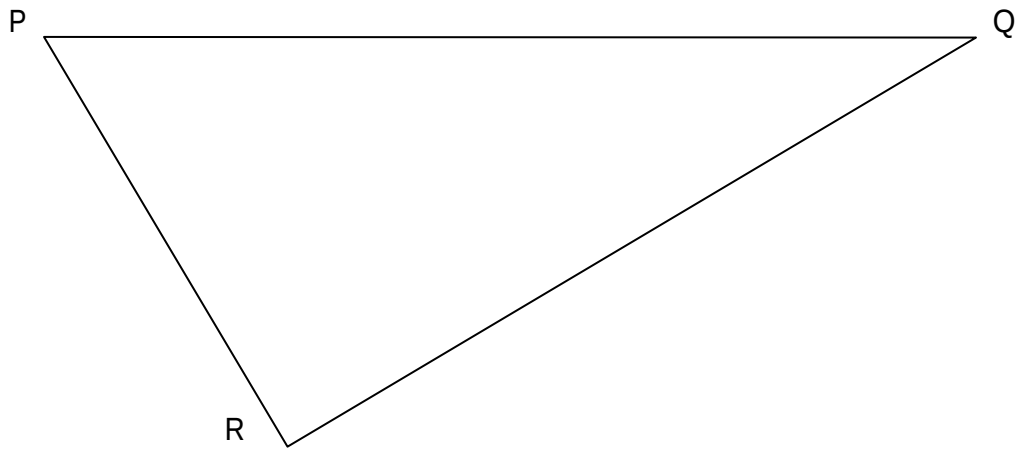
15. If the endpoints of a line segment are at *a* and *b* on a number line, write an expression for the midpoint of the segment in terms of *a* and *b*. (1 point)

16. In the figure below, C is any point between A and B, E is the midpoint of $\overline{AC}$, and F is the midpoint of $\overline{CB}$. Write a ratio comparing AB to EF. (2 points)

Constructions: Complete the following construction problems.

17. Center of Mass (2 points)

An object's center of mass is the point where the object balances in all directions. A triangle's center of mass is located at the intersection of three line segments- the line segments connecting each of the triangle's vertices with the midpoints of the triangle segments opposite the vertices. Use a compass and straight edge to locate the following triangle's center of mass. Label the center of mass, C. (3 points)

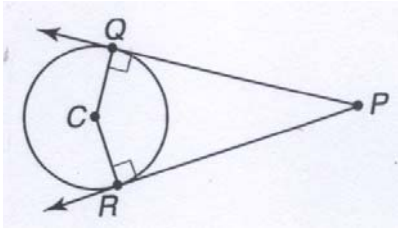


18. Oops! Broken Glass Top (2 points)

The circular glass top of your neighbor's coffee table breaks. Your neighbor is very upset and would like to replace the glass top but does not know exactly how big it was. He brings you a piece of broken glass that contains part of the boundary of the original top. He needs you to figure out how large the original glass was.

Use your compass and a straight edge to locate the center of the glass top. Then, use your compass to draw the whole circular glass top.

Hint: The center of a circle can be located by finding the intersection of two line segments which are perpendicular to lines that are tangent to the circle.



tangent- A line is tangent to a circle when it intersects the circle in exactly one point. In the figure below, $\overrightarrow{PQ}$ and $\overrightarrow{PR}$ are tangent to circle C. $\overline{QC}$ and $\overline{RC}$ are perpendicular to those rays. Their intersection is the center of the circle.